## Commutative Algebra & Algebraic Geometry $$\mathrm{SS}\ 2010$$

- (1) What can computer algebra systems like Maple or Mathematica do on algebraic curves and surfaces?
  - implicitize
  - parametrize
  - genus
  - Puiseux expansion
  - singularities
  - .....
- (2) Consider the system of algebraic equations

$$y^2 = x^3$$
,  $z = x^2$ ,  $xz = y^2$ .

Visualize the set of solutions.

(3) Is the set of solutions (over the reals R) of the system in (2) a finite set of points, a curve, a surface ? How can you determine this?