## Commutative Algebra & Algebraic Geometry SS 2010

(4) Determine a rational parametrization of the circle

$$x^2 + y^2 = 1 \ .$$

(5) Decide whether the following algebraic curve  $C_5$  defined by

$$f_5(x,y) = y^2 - x^3 + x^2 + x - 1 = 0$$

is rational (parametrizable), and if so, compute a rational parametrization:

(6) Decide whether the following algebraic curve  $C_6$  defined by

$$f_6(x,y) = y^2 - x^3 + x = 0$$

is rational (parametrizable), and if so, compute a rational parametrization:

(7) Consider the algebraic curve  $C_7$  having the rational parametrization

$$P(t) = \left(\frac{t^5+1}{t^2+3}, \frac{t^3+t+1}{t^2+1}\right) .$$

Compute the implicit defining polynomial  $f_7(x, y)$  of  $C_7$ .