

**Logic 1, WS 2006. Additional Homework 1, given Oct 12, due Oct 19**

1. Using the DeMorgan rules for quantified formulae, prove  $\neg\forall_{C[x]}\phi[x] \equiv \exists_{C[x]}\neg\phi[x]$  and its dual, where  $C[x]$  is a condition on  $x$  (like e. g.  $x$  is in a certain set), and  $\phi[x]$  is a formula containing  $x$ .
2. Prove  $\neg\bigwedge\Phi \equiv \bigvee\overline{\Phi}$ , where  $\Phi$  is a set of formulae and  $\overline{\Phi}$  is the set of the respective negated formulae.