

Logic Programming

The Basics

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 - Variables
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PROLOG

Used to solve problems involving

- objects, and
- relationships between objects.

The basics:

- Facts
- Questions
- Variables
- Conjunctions
- Rules

Relationships

Example

John owns the book

- The relationship: *ownership*
- The objects: *book*, *John*

Directional:

- John owns the book
- **Not:** The book owns John

Questions

Example

Does John own the book?

Asks a question about a relationship already established.

Rules

Describe Relationships Using other Relationships.

Example

Two people are sisters if they are both female and have the same parents.

Gives a definition of one relationship given other relationships.

- Both must be females.
- Both must have the same parents.
- If two people satisfy these rules, then they are sisters (according to our simplified relationship)

Programming in PROLOG

- **Declaring Facts** about objects and their relationships.
- **Defining Rules** about objects and their relationships.
- **Asking Questions** about objects and their relationships.

PROLOG

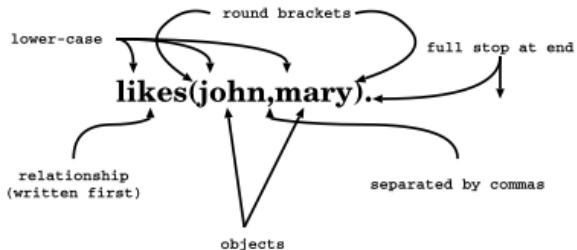
- Program can be thought of as a storehouse of facts and rules.
- Conversational Language: The user can ask questions about the set of facts and rules in the PROLOG program.

PROLOG

Sisters Example:

- A rule defining sisters and the facts about the people involved.
- The user would ask:
Are these two people sisters?
- The system would answer
yes (true) or **no** (false)

Parts of Fact



Order of Objects

```
likes(mary, john) .
```

order defined by programmer

```
mary — likes —> john
```

The fact says nothing
about how john likes mary

```
john . . . no info . . . ► mary
```

Examples of Facts

Example

Gold is valuable.

```
valuable(gold)
```

Jane is a female.

```
female(jane)
```

John owns some gold.

```
owns(john,gold)
```

John is the father of Mary.

```
father(john,mary)
```

Are these expressions really facts? Is there anything missing?

Interpretation of Names

The name refers to an object.

- **Semantic Meaning:** Given by the programmer.
- **Syntactic Meaning:** a set of characters, as PROLOG sees it.

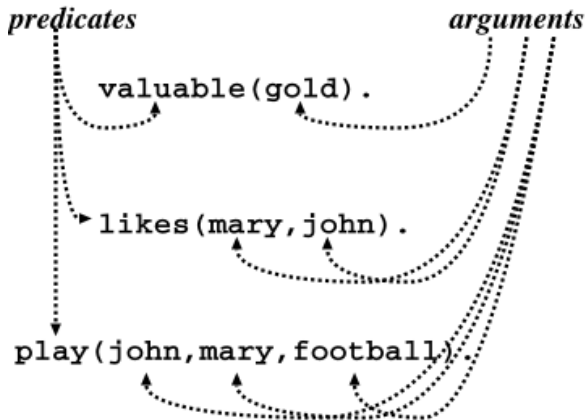
Interpretation of Names

Name refers to an object.

- Name `gold` can refer to:
 - a particular lump of gold, or
 - the chemical element Gold having atomic number 79.
- `valuable(gold)` can mean:
 - that particular lump of gold, named `gold`, is valuable, or
 - the chemical element Gold, named `gold`, is valuable.

The programmer decides (in her usage) the meaning.

Fact Terminology



Database

Definition

In PROLOG, **database** is a collection of facts.

- PROLOG draws its knowledge from these facts.
- The programmer is responsible for their accuracy.

Questions

- The database contains the facts from which the questions are answered.
- A Question can look exactly like a fact:
`owns (mary, book) .`
- The difference is in which mode one is in

Questions

In the interactive question mode (indicated by the question mark and dash `?-`):

- Question: `?- owns(mary, book) .`
- Meaning:
 - If `mary` is interpreted as a person called Mary, and `book` is interpreted as some particular book, then
 - `?- owns(mary, book) .` means: **Does Mary own the book?**

Database Search

Example

Facts in the database:

```
likes(joe, fish).  
likes(joe, mary).  
likes(mary, book).  
likes(john, book).
```

Questions:

```
?- likes(joe, money).  
no  
?- likes(joe, mary).  
yes  
?- king(john, france).  
no
```

Knowledge

The questions are always answered with respect to the database.

Example

Facts in the database:

```
human(socrates).  
human(aristotle).  
athenian(socrates).
```

Question:

Is Socrates Greek?

```
?- greek(socrates)
```

The answer with respect to this database is **No**.

Questions

Up until now questions just reflect exactly the database.

Does Mary like the book?

```
?- likes(mary,book) .
```

More Interesting Question:
What objects does Mary like?

Variables.

Variables

Tiresome to ask about every object:

```
likes(john, this)
```

```
likes(john, that)
```

Better to ask:

What does John like?

or

Does John like **X**?

(i.e. use variables)

Question With Variables

Does John like X?

```
?- likes(john, X) .
```

or

```
?- likes(john, SomethingThatJohnLikes) .
```

X and SomethingThatJohnLikes are variables.

Variable begins with a capital letter.

PROLOG Answer

Database:

```
likes(john, flowers) .
```

Question:

```
?- likes(john, X) .
```

PROLOG answers:

```
X=flowers
```


Many Answers

Database:

```
likes(john, flowers) .  
likes(john, mary) .  
likes(paul, mary) .
```

Question:

```
?- likes(john, X) .
```

PROLOG answers:

```
X=flowers  
and the user acknowledges  
X=mary  
and the user acknowledges  
no
```

Place-Marker

- The first match is found: `X=flowers`.
- The user acknowledges.
- From that place on the next match is found (the search continues).
- From the place of the last instantiation no more match was found.
- Thus answer: `no`.

Conjunctions

More Complicated Relationships:

Does Mary like John and does John like Mary?

Both Conditions must be fulfilled.

Conjunctions

Comma means Conjunction:

```
?- likes(john,mary), likes(mary, john) .
```

```
likes(mary, food) .
```

```
likes(mary, wine) .
```

```
likes(john, wine) .
```

```
likes(john, mary) .
```

Answer: no

A match for likes(john, mary)
but none for likes(mary, john)

Conjunctions with Variables

Is there anything that both mary and john like?

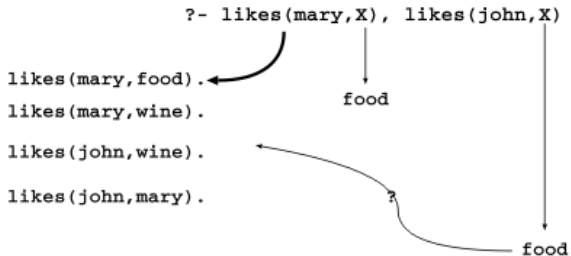
Find out what Mary likes and then see if John likes it.

```
?- likes(mary,X), likes(john,X).
```

Backtracking

- Find match for the first goal.
- Then see if matches the second.
- If not, find another match for the first.
- See if this matches the second.
- etc.

Match First



Match Second

```
?- likes(mary,X), likes(john,X)
```

likes(mary,food).
likes(mary,wine).
likes(john,wine).
likes(john,mary).

no

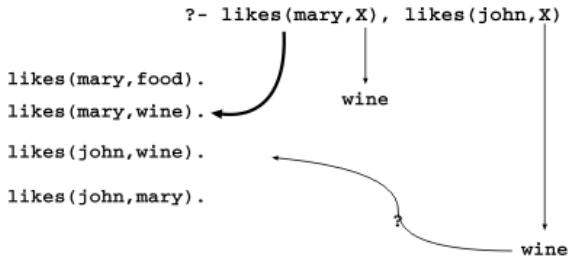
not found

food

```
graph TD
    Q["?- likes(mary,X), likes(john,X)"]
    F1["likes(mary,food)."]
    F2["likes(mary,wine)."]
    F3["likes(john,wine)."]
    F4["likes(john,mary)."]
    R1["no"]
    R2["not found"]
    R3["food"]

    Q --> F1
    Q --> F2
    Q --> F3
    Q --> F4
    F1 --> R1
    F2 --> R2
    F3 --> R2
    F4 --> R2
    R2 --> R3
```


Backtrack



Success

```
?- likes(mary,X), likes(john,X)
```

likes(mary,food).
likes(mary,wine).
likes(john,wine).
likes(john,mary).

The diagram illustrates the variable binding for the query `?- likes(mary,X), likes(john,X)`. It shows four facts: `likes(mary,food).`, `likes(mary,wine).`, `likes(john,wine).`, and `likes(john,mary).`. The variable `X` in the query is bound to `wine` for the first `likes(john,X)` and `found` for the second `likes(mary,X)`. Arrows indicate these bindings: a vertical arrow from the first `X` to `wine`, a vertical arrow from the second `X` to `wine`, a curved arrow from the `X` in `likes(mary,X)` to `found`, and a curved arrow from the `X` in `likes(john,X)` to `wine`.