# Information Systems <br> Relational Databases 

## Temur Kutsia

Research Institute for Symbolic Computation Johannes Kepler University of Linz, Austria
kutsia@risc.uni-linz.ac.at

## Outline

The Relational Model (Continues from the Previous Lecture) Data Structure. Types and Relations Data Manipulation. Relational Algebra

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## Relations

- Up to now we discussed type, values, and variables in general.
- Now: Relations types, values, and variables in particular.
- Since relations are built out of tuples, we examine tuple types, values, and variables.


## Tuples

## Tuple

- Given a collection of (not necessarily distinct) types $T_{i}, 1 \leq i \leq n$, a tuple value (or tuple) $t$ on those types is a set of ordered triples of the form $\left\langle A_{i}, T_{i}, v_{i}\right\rangle$, where
- $A_{i}$ is an attribute name, $T_{i}$ is a type name, $v_{i}$ is a value of type $T_{i}$.
- The value $n$ is the degree or arity of $t$.
- The ordered triple $\left\langle A_{i}, T_{i}, v_{i}\right\rangle$ is a component of $t$.
- The ordered pair $\left\langle A_{i}, T_{i}\right\rangle$ is an attribute of $t$ and is uniquely identified by $A_{i}$. ( $A_{i}$ 's are all distinct.)
- $v_{i}$ is the attribute value for $A_{i}$.
- $T_{i}$ is the attribute type for $A_{i}$.
- The complete set of attributes is the heading of $t$.
- The tuple type of $t$ is determined by the heading of $t$. The tuple type name is precisely TUPLE $\left\{A_{1} T_{1}, A_{2} T_{2}, \ldots, A_{n} T_{n}\right\}$.


## Tuple

## Example

Sample tuple：
\｛（MAJOR＿P\＃，P\＃，P2〉，（MINOR＿P\＃，P\＃，P4〉，〈QTY，QTY，7）\}

| MAJOR＿P\＃：P\＃ | MINOR＿P\＃：P\＃ | QTY：QTY |
| :--- | :--- | ---: |
| P2 | P4 | 7 |

－Attribute names：MAJOR＿P\＃，MINOR＿P\＃，QTY．
－The corresponding type names：P\＃，P\＃，and QTY．
－The corresponding values：P2，P4， 7 ．
－The degree of the tuple is three．
－The heading：
MAJOR＿P\＃：P\＃$\quad$ MINOR＿P\＃：P\＃$\quad$ QTY：QTY
－The type：TUPLE \｛ MAJOR＿P\＃P\＃，MINOR＿P\＃P\＃，QTY QTY\}

## Tuple

- In informal contexts type names are often omitted from a tuple heading, showing just the attribute names.
For instance, writing

| MAJOR_P\# | MINOR_P\# | QTY |
| :--- | :--- | ---: |
| P2 | P4 | 7 |

instead of

| MAJOR_P\# : P\# | MINOR_P\# : P\# | QTY : QTY |
| :--- | :--- | ---: |
| P2 | P4 | 7 |

## Tuple Properties

- Every tuple contains exactly one value for each attribute.
- The order of components of a tuple does not matter.
- Every subset (including the empty subset) of a tuple is a tuple.


## Tuple Type Generators

- Example:

VAR ADDR TUPLE \{
STREET CHAR,
CITY CHAR, STATE CHAR, ZIP CHAR \} ;

- Defines the variable ADDR to be of type TUPLE \{ STREET CHAR, CITY CHAR, STATE CHAR, ZIP CHAR \}
- Tuple selector operator:

TUPLE \{ STREET '1600 Penn. Ave.', CITY 'Washington', STATE 'DC', ZIP '20500' \}

## Operations on Tuples

Tuple equality:

- Tuples $t_{1}$ and $t_{2}$ are equal $\left(t_{1}=t_{2}\right)$ iff

1. they have the same attributes Attr $_{1}, \ldots$, Attr $_{n}$, and
2. the value $v_{i}$ of $A t t r_{i}$ in $t_{1}$ is equal to the value $v_{i}$ of $A t t r_{i}$ in $t_{2}$.

## Operations on Tuples

Assume the current value of the ADDR variable is
TUPLE \{ STREET '1600 Penn. Ave.', CITY 'Washington', STATE 'DC', ZIP '20500' \}

- Tuple projection: ADDR \{ CITY, ZIP \} denotes the tuple TUPLE \{ CITY 'Washington', ZIP '20500' \}.
- Extraction: ZIP FROM ADDR denotes '20500'.
- Tuple type inference: Tuple type of the result of ADDR \{ CITY, ZIP \} is TUPLE \{ CITY CHAR, ZIP CHAR \}.


## Operations on Tuples

## WRAP and UNWRAP:

- Consider the tuple types:

> TT1: TUPLE \{ NAME NAME, ADDR TUPLE $\{$
> STREET CHAR, CITY CHAR, STATE CHAR, ZIP CHAR \} \}.

TT2: TUPLE \{ NAME NAME, STREET CHAR, CITY CHAR, STATE CHAR, ZIP CHAR \}.

- NADDR1, NADDR2: The variables of types TT1, TT2, resp.
- The expression

NADDR2 WRAP \{STREET, CITY, STATE, ZIP\} AS ADDR takes the current value of NADDR2 and wraps STREET, CITY, STATE, ZIP components into a single tuple-valued ADDR component. The result is of of type TT1.

- The expression NADDR1 UNWRAP ADDR takes the current value of NADDR1 and unwraps ADDR into four separate components. The result is of type TT2.


## Relations

## Relation

- A relation value (or relation) $r$ consists of a heading and a body, where
- The heading of $r$ is a tuple heading. Relation $r$ has the same attributes and the same degree as that heading does.
- The body of $r$ is the set of tuples, all having that same heading; the cardinality of that set is said to be the cardinality of $r$.


## Relation type

- A relation type of $r$ is determined by the heading of $r$.
- It has the same attributes (and hence attribute names and types) and degree as that heading does.
- The relation type name is

RELATION \{ A1 T1, ..., An Tn \}

## Relations

Example

| MAJOR_P\# : P\# | MINOR_P\# : P\# | QTY : QTY |
| :--- | :--- | ---: |
| P1 | P2 | 5 |
| P1 | P3 | 3 |
| P2 | P3 | 2 |
| P2 | P4 | 7 |
| P3 | P5 | 4 |
| P4 | P6 | 8 |

Type:
RELATION \{ MAJOR_P\# : P\#, MINOR_P\# : P\#, QTY : QTY \}

## Relations

- $n$-ary relation: relation of degree $n$.
- Every subset of a heading is a heading.
- Every subset of a body is a body.


## The RELATION Type Generator

Example:

- VAR PART_STRUCTURE ...

RELATION \{ MAJOR_P\# : P\#, MINOR_P\# : P\#, QTY : QTY \}

- PART_STRUCTURE: relation variable (relvar)
- RELATION \{ MAJOR_P\# : P\#, MINOR_P\# : P\#, QTY : QTY \}: Invocation of the RELATION type generator, gives a generated type.


## Relation Properties

Within the same relation

- every tuple contains exactly one value for each attribute,
- no left-to-right ordering to the attributes,
- no top-to-bottom ordering to the tuples,
- no duplicate tuples.


## Relations with No Attributes

- Every relation has a set of attributes.
- This set, in particular, can be empty: No attributes at all.
- Does not mean the empty relation!
- Empty relation: relation with the empty body.
- Relation with no attributes: relation with the empty heading.


## Relations with No Attributes

- Relation with no attributes can contain at most one tuple, the 0-tuple.
- The 0-tuple contains no components.
- Hence, two relations of degree 0: one that contains just one tuple, and one that contains no tuples at all.
- Names: TABLE_DEE and TABLE_DUM, respectively.


## Operators on Relations

Comparisons:

- =, $\neq \subseteq, \subseteq, \subset, \supseteq, \supset$, IS_EMPTY.
- They can appear whenever a boolean expression is expected.
- Example: $\mathrm{S}\{\mathrm{CITY}\}=\mathrm{P}\{$ CITY \}: Is the projection of suppliers over CITY equal to the projection of parts over city?


## Operators on Relations

Other operators:

- Test whether the given tuple $t$ appears in a given relation $r$ : $t \in r$.
- Extracting the single tuple from a relation of cardinality one: TUPLE FROM r
- Other operators like join, restrict, project, etc. Considered in the relational algebra part.


## Operators on Relations

Relation type inference:

- Given the suppliers relvar S, the expression S \{ S\#, CITY \} yields a relation whose type is RELATION \{ S\# S\#, CITY CHAR \}


## Relation Variables

- Base and derived relvars.
- Base and derived relations.
- Other name of derived relvars: views


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- Base and derived relvars.
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## Relation Variables

## Example

Defining base relvars S, P, and SP:

VAR S BASE RELATION
\{ S\# S\#,
SNAME NAME, STATUS INTEGER, CITY CHAR \}
PRIMARY KEY \{ S\# \} ;

VAR P BASE RELATION
\{ P\# P\#,
PNAME NAME, COLOR COLOR, WEIGHT WEIGHT, CITY CHAR \}
PRIMARY KEY \{ P\# \};

VAR SP BASE RELATION
\{ S\# S\#,

P\# P\#,
QTY QTY \}
PRIMARY KEY \{ S\#, P\# \}
FOREIGN KEY \{ S\# \} REFERENCES S
FOREIGN KEY \{ P\# \} REFERENCES P

## Explanation

- The relation type of the relvar S is RELATION \{S\# S\#, SNAME NAME, STATUS INTEGER, CITY CHAR \}
- The terms heading, body, attributes, tuple, degree, etc. are interpreted to apply to relvars.
- When a base relvar is defined, it is given an initial value that is the empty relation of appropriate type.
- It is assumed that a means is available for specifying default values to some attributes of base relvars.


## Updating Relvars

- Assume S' and SP' are base relvars.
- The type of $S^{\prime}$ is the same as the type of $S$.
- The type of SP' is the same as the type of SP.
- Some valid examples of relation assignment:

1. $S^{\prime}:=S, S P^{\prime}:=S P$;
2. $\mathrm{S}^{\prime}:=\mathrm{S}$ WHERE CITY = 'London'
3. $\mathrm{S}:=\mathrm{S}$ WHERE NOT (CITY = 'Paris')

- Each assignment
(a) retrieves the relation specified on the right hand side and
(b) updates the relvar specified on the left hand side.


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## Relational Algebra

- Theoretical basis for database query languages.
- Attracted attention after Edgar F. Codd introduced the relational model in 1970-ies.
- Formal system for manipulating relations:
- Operands: relations.
- Operators: union, intersection, difference, Cartesian product, restrict, project, join, divide, rename.
- Operations operate on relations and produce relations (closure).


## Rename

- Purpose: Rename attributes within a specified relation.
- Action: Takes a given relation and returns another one that is identical to the given one except that one of its attributes has a different name.
- Example:

S | S\# | SNAME | STATUS | CITY |
| :--- | :--- | ---: | :--- |
| S1 | Smith | 20 | London |
| S2 | Jones | 10 | Paris |
| S3 | Blake | 30 | Paris |

## S RENAME CITY AS SCITY

| S\# | SNAME | STATUS | SCITY |
| :--- | :--- | ---: | :--- |
| S1 | Smith | 20 | London |
| S2 | Jones | 10 | Paris |
| S3 | Blake | 30 | Paris |

## Union

- Specification: Given two relations $a$ and $b$ of the same type, $a$ UNION $b$ is a relation of the same type, with body consisting of all tuples $t$ such that $t$ appears in $a$ or in $b$ or both.
- Example:

A | S\# | SNAME | STATUS | CITY |
| :--- | :--- | ---: | :--- |
| S1 | Smith | 20 | London |
| S4 | Clark | 20 | London |

B | S\# | SNAME | STATUS | CITY |
| :--- | :--- | ---: | :--- |
| S1 | Smith | 20 | London |
| S2 | Jones | 10 | Paris |

A UNION B

| S\# | SNAME | STATUS | CITY |
| :---: | :--- | ---: | :--- |
| S1 | Smith | 20 | London |
| S4 | Clark | 20 | London |
| S2 | Jones | 10 | Paris |

## Intersection

- Given two relations $a$ and $b$ of the same type, $a$ INTERSECT $b$ is a relation of the same type, with body consisting of all tuples $t$ such that $t$ appears in both $a$ and $b$.
- Example:

| A\# | SNAME | STATUS | CITY |
| :--- | :--- | ---: | :--- |
| S1 | Smith | 20 | London |
| S4 | Clark | 20 | London |

B | S\# | SNAME | STATUS | CITY |
| :--- | :--- | ---: | :--- |
| S1 | Smith | 20 | London |
| S2 | Jones | 10 | Paris |

A INTERSECT B

| S\# | SNAME | STATUS | CITY |
| :--- | :--- | ---: | :--- |
| S1 | Smith | 20 | London |

## Difference

- Given two relations $a$ and $b$ of the same type, $a$ MINUS $b$ is a relation of the same type, with body consisting of all tuples $t$ such that $t$ appears $a$ and not in $b$.
- Example:

| A | S | SNAME | STATUS | CITY |
| :---: | :--- | :--- | ---: | :--- |
| S1 | Smith | 20 | London |  |
| S4 | Clark | 20 | London |  |

B | S\# | SNAME | STATUS | CITY |
| :---: | :--- | ---: | :--- |
| S1 | Smith | 20 | London |
| S2 | Jones | 10 | Paris |

A MINUS B

| S\# | SNAME | STATUS | CITY |
| :---: | :--- | ---: | :--- |
| S4 | Clark | 20 | London |

## B MINUS A

| S\# | SNAME | STATUS | CITY |
| :--- | :--- | ---: | :--- |
| S2 | Jones | 10 | Paris |

## Cartesian Product

- Given two relations $a$ and $b$ without common attribute names, $a$ TIMES $b$ is a relation with a heading that is the (set theoretic) union of the heading of $a$ and $b$ and with the body consisting of the set of all tuples $t$ such that $t$ is a (set theoretic) union of a tuple appearing in $a$ and a tuple appearing in $b$.
- Example:



## Restriction

- Given a relation a with attributes $X, Y, \ldots, Z$ and a truth-valued function $p$ whose parameters are some subset of $X, Y, \ldots, Z$, the restriction of a according to $p$, a WHERE $p$, is a relation with the same heading as a and with body consisting of all those tuples in a on which $p$ evaluates to TRUE.
- Example:

| S | S\# | SNAME | STATUS | CITY |
| :---: | :--- | :--- | ---: | :--- |
| S1 | Smith | 20 | London |  |
| S2 | Jones | 10 | Paris |  |
| S3 | Blake | 30 | Paris |  |

S WHERE CITY = 'London'

| S\# | SNAME | STATUS | CITY |
| :--- | :--- | ---: | :--- |
| S1 | Smith | 20 | London |

## Restriction

- Given a relation a with attributes $X, Y, \ldots, Z$ and a truth-valued function $p$ whose parameters are some subset of $X, Y, \ldots, Z$, the restriction of a according to $p$, a WHERE $p$, is a relation with the same heading as a and with body consisting of all those tuples in a on which $p$ evaluates to TRUE.
- Example:

P| | P\# | PN | COLOR | WEIGHT | CITY |
| :--- | :--- | :--- | ---: | :--- |
|  | P1 | Nut | Red | 12.0 |
| P2 | London |  |  |  |
| Polt | Green | 17.0 | Paris |  |
| P3 | Screw | Blue | 17.0 | Oslo |
| P4 | Screw | Red | 14.0 | London |
| P5 | Cam | Blue | 12.0 | Paris |

P WHERE WEIGHT < WEIGHT (14.0)

| P\# | PN | COLOR | WEIGHT | CITY |
| :--- | :--- | :--- | ---: | :--- |
| P1 | Nut | Red | 12.0 | London |
| P5 | Cam | Blue | 12.0 | Paris |

## Restriction

- Given a relation a with attributes $X, Y, \ldots, Z$ and a truth-valued function $p$ whose parameters are some subset of $X, Y, \ldots, Z$, the restriction of a according to $p$, a WHERE $p$, is a relation with the same heading as a and with body consisting of all those tuples in a on which $p$ evaluates to TRUE.
- Example:

| SP | S\# | P\# | QTY |
| :---: | :---: | :---: | :---: |
|  | S1 | P1 | 300 |
|  | S1 | P2 | 200 |
|  | S2 | P1 | 400 |
|  | S2 | P2 | 100 |

SP WHERE S\# = S\# ('S3') or P\# = P\# ('P4')

| S\# | P\# | QTY |
| :--- | :--- | :--- |
|  |  |  |

## Projection

- Given a relation a with attributes $X, Y, \ldots, Z$, the projection of a according on $X, Y, \ldots, Z$, written $a\{X, Y, \ldots, Z\}$, is a relation with
- a heading derived from the heading of $a$ by removing all attributes that are not among $X, Y, \ldots, Z$;
- a body consisting of all tuples $\{X x, Y y, \ldots, Z z\}$ such that the tuple appears in a with $X$ value $x, Y$ value $y, \ldots$, and $Z$ value $z$.
- Example:

| S\# | SNAME | STATUS | CITY |
| :--- | :--- | ---: | :--- |
| S1 | Smith | 20 | London |
| S2 | Jones | 10 | Paris |
| S3 | Blake | 30 | Paris |

S \{ CITY \}
CITY
London
Paris

## Projection

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- a heading derived from the heading of $a$ by removing all attributes that are not among $X, Y, \ldots, Z$;
- a body consisting of all tuples $\{X x, Y y, \ldots, Z z\}$ such that the tuple appears in a with $X$ value $x, Y$ value $y, \ldots$, and $Z$ value $z$.
- Example:

| P\# | PN | COLOR | WEIGHT | CITY |  |
| :---: | :--- | :--- | :--- | ---: | :--- |
|  | P1 | Nut | Red | 12.0 | London |
| P2 | Bolt | Green | 17.0 | Paris |  |
| P3 | Screw | Blue | 17.0 | Oslo |  |
| P4 | Screw | Red | 14.0 | London |  |
|  |  |  |  |  |  |

P \{COLOR, CITY \}

| COLOR | CITY |
| :--- | :--- |
| Red | London |
| Green | Paris |
| Blue | Oslo |

## Projection

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- a heading derived from the heading of $a$ by removing all attributes that are not among $X, Y, \ldots, Z$;
- a body consisting of all tuples $\{X x, Y y, \ldots, Z z\}$ such that the tuple appears in a with $X$ value $x, Y$ value $y, \ldots$, and $Z$ value $z$.
- Example:

| S\# | SNAME | STATUS | CITY |
| :--- | :--- | ---: | :--- |
| S1 | Smith | 20 | London |
| S2 | Jones | 10 | Paris |
| S3 | Blake | 30 | Paris |

(S WHERE CITY = 'Paris') \{ S\# \}

| S\# |
| :--- |
| S2 |
| S3 |

## Join

- Let a relation a have attributes $X_{1}, \ldots, X_{m}, Y_{1}, \ldots Y_{n}$, and $b$ have the attributes $Y_{1}, \ldots Y_{n}, Z_{1}, \ldots, Z_{p}$.
- The (natural) join of $a$ and $b$, denoted $a$ JOIN $b$ is a relation with heading $X_{1}, \ldots, X_{m}, Y_{1}, \ldots, Y_{n}, Z_{1}, \ldots, Z_{p}$ and body consisting of all tuples $X_{1} x_{1}, \ldots, X_{m} x_{m}, Y_{1} y_{1}, \ldots, Y_{n} y_{n}, Z_{1} z_{1}, \ldots, Z_{p} z_{p}$ such that
- a tuple appears in a with $X_{i}$ value $x_{i}$, and $Y_{j}$ value $y_{j}$ for all $1 \leq i \leq m$ and $1 \leq j \leq n$, and
- a tuple appears in $b$ with $Y_{j}$ value $y_{j}$ and $Z_{k}$ value $z_{k}$ for all $1 \leq j \leq n$ and $1 \leq k \leq p$.


## Join. Example

| S\# | SNAME | ST | CITY |
| :---: | :--- | :--- | :--- |
| S1 | Smith | 20 | London |
| S2 | Jones | 10 | Paris |
| S3 | Blake | 30 | Paris |


| P\# | PN | COLOR | WGT | CITY | P |
| :--- | :--- | :--- | ---: | :--- | :--- |
| P1 | Nut | Red | 12.0 | London |  |
| P2 | Bolt | Green | 17.0 | Paris |  |
| P3 | Screw | Blue | 17.0 | Oslo |  |
| P4 | Screw | Red | 14.0 | London |  |
| P5 | Cam | Blue | 12.0 | Paris |  |
| Saln |  |  |  |  |  |


| S\# | SNAME | ST | CITY | P\# | PN | COLOR | WGT |
| :--- | :--- | :--- | ---: | :--- | :--- | :--- | :--- |
| S1 | Smith | 20 | London | P1 | Nut | Red | 12.0 |
| S1 | Smith | 20 | London | P4 | Screw | Red | 14.0 |
| S2 | Jones | 10 | Paris | P2 | Bolt | Green | 17.0 |
| S2 | Jones | 10 | Paris | P5 | Cam | Blue | 12.0 |
| S3 | Blake | 30 | Paris | P2 | Bolt | Green | 17.0 |
| S3 | Blake | 30 | Paris | P5 | Cam | Blue | 12.0 |

## Divide

- Let a relation a have attributes $X_{1}, \ldots, X_{m}$ and $b$ have the attributes $Y_{1}, \ldots Y_{n}$ such that no $X_{i}$ has the same name as any $Y_{j}$, and
- let a relation $c$ have the attributes $X_{1}, \ldots, X_{m}, Y_{1}, \ldots Y_{n}$.
- The division of $a$ by $b$ per c (a dividend, $b$ divisor, $c$ mediator), denoted a DIVIDEBY $b$ PER $c$ is a relation with heading $X_{1}, \ldots, X_{m}$ and body consisting of all tuples $X_{1} x_{1}, \ldots, X_{m} x_{m}$ appearing in a such that a tuple $X_{1} x_{1}, \ldots, X_{m} x_{m}, Y_{1} y_{1}, \ldots, Y_{n} y_{n}$ appears in $c$ for all tuples $Y_{1} y_{1}, \ldots, Y_{n} y_{n}$ appearing in $b$.


## Divide. Example

| DEND | S\# S1 S2 S3 S4 S5 | MED | S\# <br> S1 <br> S1 <br> S1 <br> S1 <br> S1 <br> S1 <br> S1 <br> .. | P\# P1 P2 P3 P4 P5 P6 .. | S2 <br> S2 <br> S3 <br> S3 <br> S4 <br> S4 <br> S4 | P1 <br> P2 <br> P2 <br> P2 <br> P4 <br> P5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| DOR | P\# | DOR | P\# |  | DOR | P\# |
|  | P1 |  | P2 |  |  | P1 |
|  |  |  | P4 |  |  | P2 |
|  |  |  |  |  |  | P3 |
|  |  |  |  |  |  | P5 |
| DEND | DIVE | BY DOR | PER | MED |  | P6 |


| S\# |
| :--- | :--- |
| S1 |
| S2 |$\quad$| S\# |
| :--- |
| S1 |
| S4 |$\quad$| S1 |
| :--- |

## Examples. Supplier-and-Parts

- Get supplier names for suppliers who supply part P2.
- ( ( SP JOIN S ) WHERE P\# = P\# ('P2')) \{ SNAME \}
- SP JOIN S extends which SP tuple with the corresponding supplier information (SNAME, STATUS, CITY values). The result is restricted to just those tuples for part P2. The restriction is projected over SNAME


## Examples. Supplier-and-Parts

- Get supplier names for suppliers who supply at least one red part.
- ( ( ( P WHERE COLOR = COLOR('Red') )

JOIN SP ) \{ S\# \} JOIN S ) \{ SNAME \}

## Examples. Supplier-and-Parts

- Get supplier names for suppliers who supply all parts.
- ( ( S \{ S\#\} DIVIDEBY P \{ P\#\} PER SP \{ S\#, P\# \} ) JOIN S) \{ SNAME \}


## Examples. Supplier-and-Parts

- Get supplier numbers for suppliers who supply at least all those parts supplied by supplier S2.
- S \{ S\# \} DIVIDEBY ( SP WHERE S\# = S\# ('S2') ) \{P\#\}

PER SP \{S\#, P\#\})

## Examples. Supplier-and-Parts

- Get all pairs of supplier numbers such that the suppliers are located in the same city.
- ( ( ( S RENAME S\# AS SA ) \{ SA, CITY \} JOIN ( S RENAME S\# AS SB ) \{ SB, CITY \} ) WHERE SA < SB \{ SA, SB \}


## Examples. Supplier-and-Parts

- Get supplier names for suppliers who do not supply part P2.
- ( ( S \{ S\# \} MINUS ( SP WHERE P\# = P\# ('P2') ) \{S\#\} ) JOIN S )\{ SNAME \}

