Logic Programming Prolog as Language

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Prolog as Language

- Syntax
- Operators
- Equality
- Arithmetic
- Satisfying Goals

Syntax

Terms:

- constant
- variable
- structure

Constants

- Naming (specific objects, specific relationships)
 - likes mary john book wine owns jewels can_steal
 - ▶ a
 - ▶ void
 - **=**
 - ▶ 'george-smith'
 - **▶** -->
 - ▶ george_smith
 - ▶ ieh2304
- Integers (size is implementation dependent)

Non-Constants

The following symbols are not constants:

- ▶ 2340ieh Begins with number.
- george-smith Contains dash.
- Void Begins with capital.
- ► _alpha Begins with underscore.

Variables

Begin with capital or with underscore:

- Answer
- Input
- _3_blind_mice

Anonymous variable: A single underscore

- ▶ likes(john,_).
- Need not be assigned to the same variable likes (_,_).

Structures

- Collection of Objects, Components, grouped together in one object.
- Help Organize.
- Make code more readable.

Structures

Example: Index Card for Library

- Author's Name
- ▶ Title
- Date
- Publisher
- Name could be split also first, last, etc.

Examples

- owns(john,book).
- One Level: owns (john, wuthering_heights). owns (mary, moby_dick).
- Deeper: owns (john, book (wuthering_heights, bronte)).
 - owns (john, book (wuthering heights, author (emily, bronte))).

Questions

- ▶ Does John own a book by the Bronte sisters? owns (john, book (X, author (Y, bronte))).
- ► For the yes/no question
 owns (john, book (_, author (_, bronte))).
 (note that each _ could be different)

Equality

An infix operator =

- X = Y
 A match is attempted between expression X and expression Y
- PROLOG does what it can to match X and Y

Example: Instantiated

- X is uninstantiated.
- Y is an object.
- X = Y: X and Y will be matched.
- Thus X will be instantiated by the object Y.

```
?- rides(man,bicycle) = X.
X = rides(man,bicycle);
```

Example: Symbols

```
?- policeman = policeman.
Yes
?- paper = pencil.
No
?-1066 = 1066.
Yes
?-1206 = 1583.
No
```

Arguments Instantiated

If the structures are equal then their arguments are matched.

```
?- rides(man,bicycle) = rides(man,X).
X = bicycle;
```

Arguments Instantiated

```
?- a(b,C,d(e,F,g(h,i,J))) =
    a(B,c,d(E,f,g(H,i,j))).

B = b
C = c
E = e
F = f
H = h
J = j;
```

Equality

```
?- X=X.

X = _G147;

No

?- Y=X.

Y = _G147;

X = _G147;
```

Equality

```
?- X=Y, X=1200.

X = 1200

Y = 1200;

No

?-
```

Arithmetic Comparisons

$$X = Y$$

$$X = < Y$$

$$X >= Y$$

Arithmetic

```
?- 123 > 14.
Yes
?- 14 > 123.
No
?- 123 > X.
ERROR: Arguments are not sufficiently instantiated
?-
```

Example

► Prince was a prince during year, Year if
Prince reigned between years Begin and End, and
Year is between Begin and End.

```
prince(Prince, Year) :-
       reigns (Prince, Begin, End),
       Year >= Begin,
       Year = < End.
reigns (rhodri, 844, 878).
reigns (anarawd, 878, 916).
reigns (hywel_dda, 916, 950).
reigns (lago_ad_idwal, 950, 979).
reigns (hywel_ab_ieuaf, 979, 985).
reigns (cadwallon, 985, 986).
reigns (maredudd, 986, 999).
```

Runs

- ▶ Was Cadwallon a prince in 986?
- ▶ Is Rhodri a prince in 1995?

```
?- prince(cadwallon,986).
Yes
?- prince(rhodri,1995).
No
?-
```

Who was a Prince When

- ▶ Who was the prince in 900?
- ▶ Who was the prince in 979?

```
?- prince (Prince, 900).
Prince = anarawd;
No
?- prince (Prince, 979).
Prince = lago ad idwal ;
Prince = hywel_ab_ieuaf ;
No
?-
```

Invalid Question

When was Cadwallon a prince?

?- prince(cadwallon, Year).
ERROR: Arguments are not sufficiently
instantiated

Calculating

Calculating the Population Density of a Country: Population over the Area

```
density (Country, Density) :-
       pop (Country, Pop),
       area (Country, Area),
       Density is Pop/Area.
pop (usa, 305).
pop (india, 1132).
pop (china, 1321).
pop (brazil, 187).
area (usa, 3).
area(india,1).
area(china, 4).
area (brazil, 3).
```

Questions

▶ What is the population density of USA?

```
?- density(usa, X).
X = 101.667;
```

Questions

What Country has which density?

```
?- density(X,Y).
X = usa
Y = 101.667;
X = india
Y = 1132;
X = china
Y = 330.25;
X = brazil
Y = 62.3333;
No
?-
```

Arithmetic Operations

```
X + Y
X - Y
X * Y
X / Y
X mod Y
```

How Prolog Answers Questions

```
Program:
female (mary).
parent (C, M, F):-mother (C, M), father (C, F).
mother (john, ann).
mother (mary, ann).
father (mary, fred).
father (john, fred).
Question:
?-female(mary), parent(mary, M, F), parent(john, M, F).
```

How does it work?

Matching

- ➤ An uninstantiated variable will match any object. That object will be what the variable stands for.
- An integer or atom will only match itself.
- A structure will match another structure with the same functor and the same number of arguments and all corresponding arguments must match

How Is this Matched

```
?- sum(X+Y) = sum(2+3).

X = 2,

Y = 3
```