

Logic Programming

The Basics

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Contents

Basics of PROLOG

Facts

Questions

Variables

Conjunction

Rules

PROLOG

Used to solve problems involving

- ▶ objects, and
- ▶ relationships between objects.

Relationships

Example

John owns the book

- ▶ The relationship: *ownership*
- ▶ The objects: *book, John*

Directional:

- ▶ John owns the book
- ▶ **Not:** The book owns John

Questions

Example

Does John own the book?

Asks a question about a relationship already established.

Rules

Describe Relationships Using other Relationships.

Example

Two people are sisters if they are both female and have the same parents.

Gives a definition of one relationship given other relationships.

- ▶ Both must be females.
- ▶ Both must have the same parents.
- ▶ If two people satisfy these rules, then they are sisters (according to our simplified relationship)

Programming in PROLOG

- ▶ **Declaring Facts** about objects and their relationships.
- ▶ **Defining Rules** about objects and their relationships.
- ▶ **Asking Questions** about objects and their relationships.

PROLOG

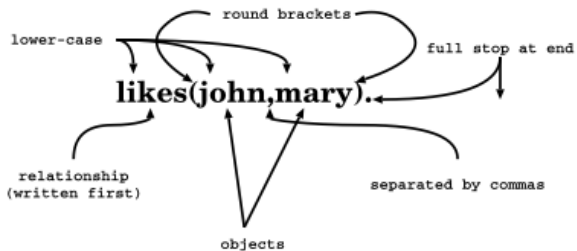
- ▶ Program can be thought of as a storehouse of facts and rules.
- ▶ Conversational Language: The user can ask questions about the set of facts and rules in the PROLOG program.

PROLOG

Sisters Example:

- ▶ A rule defining sisters and the facts about the people involved.
- ▶ The user would ask:
Are these two people sisters?
- ▶ The system would answer
yes (true) or **no** (false)

Parts of Fact



Order of Objects

`likes(mary, john) .`

order defined by programmer

`mary` $\xrightarrow{\text{likes}}$ `john`

The fact says nothing
about how john likes mary

`john . . . no info . . .` \blacktriangleright `mary`

Examples of Facts

Example

Gold is valuable.

`valuable(gold)`

Jane is a female.

`female(jane)`

John owns some gold.

`owns(john, gold)`

John is the father of Mary.

`father(john, mary)`

Examples of Facts

Example

Gold is valuable.

`valuable(gold)`

Jane is a female.

`female(jane)`

John owns some gold.

`owns(john, gold)`

John is the father of Mary.

`father(john, mary)`

Are these expressions really facts? Is there anything missing?

Interpretation of Names

The name refers to an object.

- ▶ **Semantic Meaning:** Given by the programmer.
- ▶ **Syntactic Meaning:** a set of characters, as PROLOG sees it.

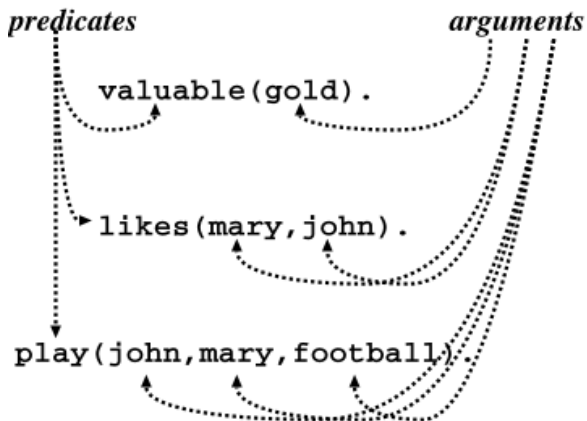
Interpretation of Names

Name refers to an object.

- ▶ Name `gold` can refer to:
 - ▶ a particular lump of gold, or
 - ▶ the chemical element Gold having atomic number 79.
- ▶ `valuable(gold)` can mean:
 - ▶ that particular lump of gold, named `gold`, is valuable, or
 - ▶ the chemical element Gold, named `gold`, is valuable.

The programmer decides (in her usage) the meaning.

Fact Terminology



Database

Definition

In PROLOG, **database** is a collection of facts.

- ▶ PROLOG draws its knowledge from these facts.
- ▶ The programmer is responsible for their accuracy.

Questions

- ▶ The database contains the facts from which the questions are answered.
- ▶ A Question can look exactly like a fact:
`owns (mary, book) .`
- ▶ The difference is in which mode one is in

Questions

In the interactive question mode (indicated by the question mark and dash ?-):

- ▶ Question: ?- owns(mary, book) .
- ▶ Meaning:
 - ▶ If `mary` is interpreted as a person called Mary, and `book` is interpreted as some particular book, then
 - ▶ ?- owns(mary, book) . means: **Does Mary own the book?**

Database Search

Example

Facts in the database:

```
likes(joe, fish) .
```

```
likes(joe, mary) .
```

```
likes(mary, book) .
```

```
likes(john, book) .
```

Questions:

```
?- likes(joe, money) .
```

no

```
?- likes(joe, mary) .
```

yes

```
?- king(john, france) .
```

no

Knowledge

The questions are always answered with respect to the database.

Example

Facts in the database:

```
human(socrates) .  
human(aristotle) .  
athenian(socrates) .
```

Question:

Is Socrates Greek?

```
?- greek(socrates)
```

The answer with respect to this database is **No**.

Questions

Up until now questions just reflect exactly the database.

Does Mary like the book?

```
?- likes(mary,book) .
```

More Interesting Question:
What objects does Mary like?

Variables.

Variables

Tiresome to ask about every object:

```
likes(john, this)
```

```
likes(john, that)
```

Better to ask:

What does John like?

or

Does John like **X**?

(i.e. use variables)

Question With Variables

Does John like X?

```
?- likes(john, X) .
```

or

```
?- likes(john, SomethingThatJohnLikes) .
```

X and SomethingThatJohnLikes are variables.

Variable begins with a capital letter.

PROLOG Answer

Database:

```
likes(john, flowers) .
```

Question:

```
?- likes(john, X) .
```

PROLOG answers:

```
X=flowers
```

Many Answers

Database:

likes(john, flowers) .

likes(john, mary) .

likes(paul, mary) .

Question:

?- likes(john, X) .

PROLOG answers:

X=flowers

and the user acknowledges

X=mary

and the user acknowledges

no

Placemark

- ▶ The first match is found: `X=flowers`.
- ▶ The user acknowledges.
- ▶ From that place on the next match is found (the search continues).
- ▶ From the place of the last instantiation no more match was found.
- ▶ Thus answer: `no`.

Conjunctions

More Complicated Relationships:

Does Mary like John and does John like Mary?

Both Conditions must be fulfilled.

Conjunctions

Comma means Conjunction:

?- likes(john,mary), likes(mary, john) .

likes(mary, food) .

likes(mary, wine) .

likes(john, wine) .

likes(john, mary) .

Answer: no

A match for likes(john, mary)

but none for likes(mary, john)

Conjunctions with Variables

Is there anything that both mary and john like?

Find out what Mary likes and then see if John likes it.

```
?- likes(mary,X), likes(john,X).
```

Backtracking

- ▶ Find match for the first goal.
- ▶ Then see if it matches the second.
- ▶ If not, find another match for the first.
- ▶ See if this matches the second.
- ▶ etc.

Match First

```
?- likes(mary,X), likes(john,X)
```

likes(mary,food). ←

likes(mary,wine). ←

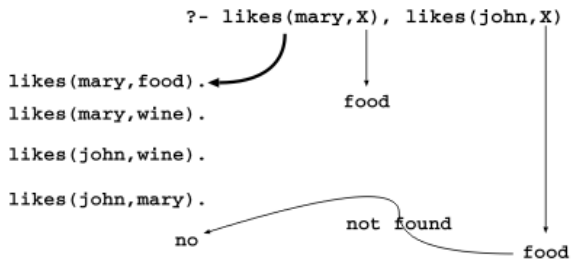
likes(john,wine). ←

likes(john,mary). ←

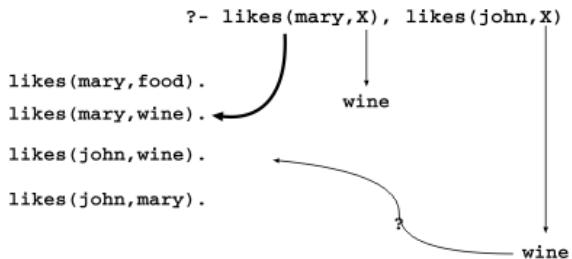
food

food

Match Second



Backtrack



Success

```
?- likes(mary,X), likes(john,X)
```

likes(mary,food).
likes(mary,wine).
likes(john,wine).
likes(john,mary).

wine

wine

found

Rules

- ▶ How to express that John likes all people?

Rules

- ▶ How to express that John likes all people?
- ▶ Listing all people?

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- ▶ Listing all people?
 - ▶ `likes(john,alfred) .`

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- ▶ How to express that John likes all people?
- ▶ Listing all people?
 - ▶ `likes(john,alfred) .`
 - ▶ `likes(john,bertrand) .`

Rules

- ▶ How to express that John likes all people?
- ▶ Listing all people?
 - ▶ `likes(john,alfred).`
 - ▶ `likes(john,bertrand).`
 - ▶ `likes(john,charles).`

Rules

- ▶ How to express that John likes all people?
- ▶ Listing all people?
 - ▶ `likes(john,alfred) .`
 - ▶ `likes(john,bertrand) .`
 - ▶ `likes(john,charles) .`
 - ▶ `likes(john,david) .`
 - ▶ **etc.**

Rules

- ▶ How to express that John likes all people?
- ▶ Listing all people?
 - ▶ `likes(john,alfred) .`
 - ▶ `likes(john,bertrand) .`
 - ▶ `likes(john,charles) .`
 - ▶ `likes(john,david) .`
 - ▶ `etc.`
- ▶ Not feasible. More compact way: Using **rules**.
John likes any object provided it is a person.

Rule Examples

- ▶ Rules state Dependence:
I use an umbrella **if** there is rain.

Rule Examples

- ▶ Rules state Dependence:
I use an umbrella **if** there is rain.
- ▶ Rules Define:
X is a bird **if** X is an animal and X has feathers.

Formulating Rules

- ▶ John likes anyone who likes wine.

Formulating Rules

- ▶ John likes anyone who likes wine.
- ▶ John likes any something if it likes wine.

Formulating Rules

- ▶ John likes anyone who likes wine.
- ▶ John likes any something if it likes wine.
- ▶ John likes X if X likes wine.

Rule Syntax

$\underbrace{\text{likes}(\text{john}, X)}_{\text{head}} \text{ :- } \underbrace{\text{likes}(X, \text{wine})}_{\text{body}}.$

rule delimiter

The diagram illustrates the syntax of a Prolog rule. The rule is written as `likes(john, X) :- likes(X, wine).`. The text `likes(john, X)` is underlined with a bracket and labeled "head". The text `likes(X, wine)` is underlined with a bracket and labeled "body". The text `:-` is labeled "rule delimiter" with an arrow pointing to it. The period `.` at the end of the rule is not labeled.

Variable Scope

The occurrences of x within a rule:

```
likes(john, X) :- likes(X, wine),  
                 likes(X, food) .
```

Variable Scope

The occurrences of x within a rule:

instantiates here
↓

```
likes (john, X) :- likes (X, wine),  
                  likes (X, food) .
```

Variable Scope

The occurrences of x within a rule:

instantiates here

↓

```
likes (john, X) :- likes (X, wine),  
                  likes (X, food) .
```

↑

checked here

Variable Scope

The occurrences of `x` within a rule:

```
likes (john, X) :- likes (X, wine),  
likes (X, food) .
```

↑ returns here

instantiates here
↓

↑ checked here

Royal Parents

Example

- ▶ The parents of X are Y and Z.
- ▶ Y is the mother.
- ▶ Z is the father.

Database:

```
male(albert) .  
male(edward) .  
female(alice) .  
female(victoria) .  
parents(edward,victoria,albert) .  
parents(alice,victoria,albert) .
```

Sisters

Example

X is a sister of Y if:

Sisters

Example

X is a sister of Y if:

- ▶ X is female,

Sisters

Example

X is a sister of Y if:

- ▶ X is female,
- ▶ X has parents M and F,

Sisters

Example

X is a sister of Y if:

- ▶ X is female,
- ▶ X has parents M and F,
- ▶ Y has parents M and F.

Sisters

Example

X is a sister of Y if:

- ▶ X is female,
- ▶ X has parents M and F,
- ▶ Y has parents M and F.

Rule:

```
sister(X,Y) :-  
    female(X),  
    parents(X,M,F),  
    parents(Y,M,F).
```

Sisters Question

Rule:

```
sister(X,Y) :-  
    female(X),  
    parents(X,M,F),  
    parents(Y,M,F).
```

Question:

```
sister(alice,edward).
```

Sisters Question

Rule:

```
sister(X,Y) :-  
    female(X),  
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Question:

```
sister(alice,edward).
```

- ▶ The question (goal) matches the head of the rule, if one replaces `X` with `alice` and `Y` with `edward`.

Sisters Question

Rule:

```
sister(X, Y) :-  
    female(X),  
    parents(X, M, F),  
    parents(Y, M, F).
```

Question:

```
sister(alice, edward).
```

- ▶ The question (goal) matches the head of the rule, if one replaces `X` with `alice` and `Y` with `edward`.
- ▶ The instance of the body becomes a new goal:

```
female(alice),  
parents(alice, M, F),  
parents(edward, M, F).
```

Is Alice Edward's Sister?

```
sister(alice,edward)
```

- (1) male(albert).
- (2) male(edward).
- (3) female(alice).
- (4) female(victoria).
- (5) parents(edward,
victoria,
albert).
- (6) parents(alice,
victoria,
albert).
- (7) sister(X,Y):-
female(X),
parents(X,M,F),
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female(X0),
parents(X0,M0,F0),
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Is Alice Edward's Sister?

- (1) `male(albert).`
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- (5) `parents(edward,`
 `victoria,`
 `albert).`
- (6) `parents(alice,`
 `victoria,`
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- (7) **`sister(X0,Y0):-`**
 `female(X0),`
 `parents(X0,M0,F0),`
 `parents(Y0,M0,F0).`

`sister(alice,edward)`

↓
`X0=alice,`
`Y0=edward`

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```
7 sister(alice,edward)
      | X0=alice,
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female(alice),
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parents(edward,M0,F0).
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7 sister(alice,edward)
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  | X0=alice,  
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parents(edward,M0,F0).
```

```
  ↓
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7 sister(alice,edward)
    ↓ X0=alice,
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    ↓
parents(alice,M0,F0),
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    |
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  parents(edward,M0,F0).
    |
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7 `sister(alice,edward)`

↓ `X0=alice,
Y0=edward`

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↓

6 `parents(alice,M0,F0),
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↓ `M0=victoria,
F0=albert`

`parents(edward,victoria,albert).`

Is Alice Edward's Sister?

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3 female(alice),
  parents(alice,M0,F0),
  parents(edward,M0,F0).
    |
    v
6 parents(alice,M0,F0),
  parents(edward,M0,F0).
    |
    | M0=victoria,
    | F0=albert
    |
    v
5 parents(edward,victoria,albert).
    |
    v
    ■
```

Who's Sister Is Alice?

```
sister(alice,X)
```

- (1) male(albert).
- (2) male(edward).
- (3) female(alice).
- (4) female(victoria).
- (5) parents(edward,
victoria,
albert).
- (6) parents(alice,
victoria,
albert).
- (7) sister(X,Y):-
female(X),
parents(X,M,F),
parents(Y,M,F).

Who's Sister Is Alice?

sister(alice,X)

- (1) male(albert).
- (2) male(edward).
- (3) female(alice).
- (4) female(victoria).
- (5) parents(edward,
 victoria,
 albert).
- (6) parents(alice,
 victoria,
 albert).
- (7) sister(X,Y):-
 female(X),
 parents(X,M,F),
 parents(Y,M,F).

Who's Sister Is Alice?

sister(alice,X)

- (1) male(albert).
- (2) male(edward).
- (3) female(alice).
- (4) female(victoria).
- (5) parents(edward,
 victoria,
 albert).
- (6) parents(alice,
 victoria,
 albert).
- (7) **sister(X,Y):-**
 female(X),
 parents(X,M,F),
 parents(Y,M,F).

Who's Sister Is Alice?

sister(alice,X)

- (1) male(albert).
- (2) male(edward).
- (3) female(alice).
- (4) female(victoria).
- (5) parents(edward,
victoria,
albert).
- (6) parents(alice,
victoria,
albert).
- (7) **sister(X0,Y0):-**
 female(X0),
 parents(X0,M0,F0),
 parents(Y0,M0,F0).

Who's Sister Is Alice?

- (1) `male(albert).`
- (2) `male(edward).`
- (3) `female(alice).`
- (4) `female(victoria).`
- (5) `parents(edward,`
 `victoria,`
 `albert).`
- (6) `parents(alice,`
 `victoria,`
 `albert).`
- (7) **`sister(X0,Y0):-`**
 `female(X0),`
 `parents(X0,M0,F0),`
 `parents(Y0,M0,F0).`

sister(alice,X)

↓ $X0=alice,$
 $Y0=X$

Who's Sister Is Alice?

- (1) male(albert).
- (2) male(edward).
- (3) female(alice).
- (4) female(victoria).
- (5) parents(edward,
victoria,
albert).
- (6) parents(alice,
victoria,
albert).
- (7) sister(X0,Y0):-
 female(X0),
 parents(X0,M0,F0),
 parents(Y0,M0,F0).

7 sister(alice,X)

↓ X0=alice,
 Y0=X

female(alice),
parents(alice,M0,F0),
parents(X,M0,F0).

Who's Sister Is Alice?

- (1) `male(albert).`
- (2) `male(edward).`
- (3) `female(alice).`
- (4) `female(victoria).`
- (5) `parents(edward,
victoria,
albert).`
- (6) `parents(alice,
victoria,
albert).`
- (7) `sister(X,Y):-
female(X),
parents(X,M,F),
parents(Y,M,F).`

7 `sister(alice,X)`

↓ `X0=alice,
Y0=X`

female(alice),
`parents(alice,M0,F0),`
`parents(X,M0,F0).`

Who's Sister Is Alice?

- (1) `male(albert).`
- (2) `male(edward).`
- (3) **`female(alice).`**
- (4) `female(victoria).`
- (5) `parents(edward,
victoria,
albert).`
- (6) `parents(alice,
victoria,
albert).`
- (7) `sister(X,Y):-
female(X),
parents(X,M,F),
parents(Y,M,F).`

7 `sister(alice,X)`

↓ `X0=alice,
Y0=X`

`female(alice),`
`parents(alice,M0,F0),`
`parents(X,M0,F0).`

Who's Sister Is Alice?

- (1) `male(albert).`
- (2) `male(edward).`
- (3) **`female(alice).`**
- (4) `female(victoria).`
- (5) `parents(edward,
victoria,
albert).`
- (6) `parents(alice,
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- (7) `sister(X,Y):-
female(X),
parents(X,M,F),
parents(Y,M,F).`

7 `sister(alice,X)`

↓ `X0=alice,
Y0=X`

`female(alice),`
`parents(alice,M0,F0),`
`parents(X,M0,F0).`

↓

Who's Sister Is Alice?

```
(1) male(albert).
(2) male(edward).
(3) female(alice).
(4) female(victoria).
(5) parents(edward,
            victoria,
            albert).
(6) parents(alice,
            victoria,
            albert).
(7) sister(X,Y):-
    female(X),
    parents(X,M,F),
    parents(Y,M,F).
```

```
7 sister(alice,X)
      ↓
      X0=alice,
      Y0=X
3 female(alice),
  parents(alice,M0,F0),
  parents(X,M0,F0).
      ↓
parents(alice,M0,F0),
parents(X,M0,F0).
```


Who's Sister Is Alice?

- (1) male(albert).
- (2) male(edward).
- (3) female(alice).
- (4) female(victoria).
- (5) parents(edward,
victoria,
albert).
- (6) parents(alice,
victoria,
albert).
- (7) sister(X,Y):-
female(X),
parents(X,M,F),
parents(Y,M,F).

```
7 sister(alice,X)
      ↓
      X0=alice,
      Y0=X
3 female(alice),
  parents(alice,M0,F0),
  parents(X,M0,F0).
      ↓
parents(alice,M0,F0),
  parents(X,M0,F0).
```

Who's Sister Is Alice?

- (1) `male(albert).`
- (2) `male(edward).`
- (3) `female(alice).`
- (4) `female(victoria).`
- (5) `parents(edward,
victoria,
albert).`
- (6) **`parents(alice,
victoria,
albert).`**
- (7) `sister(X,Y):-
female(X),
parents(X,M,F),
parents(Y,M,F).`

```
7 sister(alice,X)
      ↓
      X0=alice,
      Y0=X
3 female(alice),
  parents(alice,M0,F0),
  parents(X,M0,F0).
      ↓
parents(alice,M0,F0),
  parents(X,M0,F0).
```

Who's Sister Is Alice?

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(1) male(albert).
(2) male(edward).
(3) female(alice).
(4) female(victoria).
(5) parents(edward,
            victoria,
            albert).
(6) parents(alice,
        victoria,
        albert).
(7) sister(X,Y):-
    female(X),
    parents(X,M,F),
    parents(Y,M,F).
```

```
7 sister(alice,X)
      ↓
      X0=alice,
      Y0=X
3 female(alice),
  parents(alice,M0,F0),
  parents(X,M0,F0).
      ↓
parents(alice,M0,F0),
  parents(X,M0,F0).
      ↓
      M0=victoria
      F0=albert
```

Who's Sister Is Alice?

```
(1) male(albert).
(2) male(edward).
(3) female(alice).
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            victoria,
            albert).
(6) parents(alice,
            victoria,
            albert).
(7) sister(X,Y):-
    female(X),
    parents(X,M,F),
    parents(Y,M,F).
```

```
7 sister(alice,X)
      ↓
      X0=alice,
      Y0=X
3 female(alice),
  parents(alice,M0,F0),
  parents(X,M0,F0).
      ↓
6 parents(alice,M0,F0),
  parents(X,M0,F0).
      ↓
      M0=victoria
      F0=albert
parents(X,victoria,albert).
```

Who's Sister Is Alice?

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(1) male(albert).
(2) male(edward).
(3) female(alice).
(4) female(victoria).
(5) parents(edward,
    victoria,
    albert).
(6) parents(alice,
    victoria,
    albert).
(7) sister(X,Y):-
    female(X),
    parents(X,M,F),
    parents(Y,M,F).
```

```
7 sister(alice,X)
    ↓
    X0=alice,
    Y0=X
3 female(alice),
  parents(alice,M0,F0),
  parents(X,M0,F0).
    ↓
6 parents(alice,M0,F0),
  parents(X,M0,F0).
    ↓
    M0=victoria
    F0=albert
parents(X,victoria,albert).
```

Who's Sister Is Alice?

```
(1) male(albert).
(2) male(edward).
(3) female(alice).
(4) female(victoria).
(5) parents(edward,
            victoria,
            albert).
(6) parents(alice,
            victoria,
            albert).
(7) sister(X,Y):-
    female(X),
    parents(X,M,F),
    parents(Y,M,F).
```

```
7 sister(alice,X)
    ↓
  X0=alice,
  Y0=X
3 female(alice),
  parents(alice,M0,F0),
  parents(X,M0,F0).
    ↓
6 parents(alice,M0,F0),
  parents(X,M0,F0).
    ↓
  M0=victoria
  F0=albert
5 parents(X,victoria,albert).
    ↓
  X=edward
```

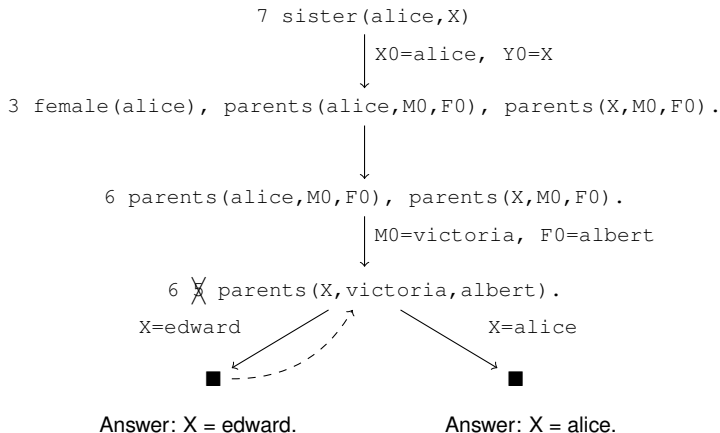
Who's Sister Is Alice?

```
(1) male(albert).
(2) male(edward).
(3) female(alice).
(4) female(victoria).
(5) parents(edward,
            victoria,
            albert).
(6) parents(alice,
            victoria,
            albert).
(7) sister(X,Y):-
    female(X),
    parents(X,M,F),
    parents(Y,M,F).
```

```
7 sister(alice,X)
      ↓
      X0=alice,
      Y0=X
3 female(alice),
  parents(alice,M0,F0),
  parents(X,M0,F0).
      ↓
6 parents(alice,M0,F0),
  parents(X,M0,F0).
      ↓
      M0=victoria
      F0=albert
5 parents(X,victoria,albert).
      ↓
      X=edward
      ■
```

Answer: X = edward.

Complete Derivation Tree



Stealing

- ▶ The Rule:

A person may steal something if the person is a thief and he likes the thing.

- ▶ Prolog Rule:

```
may_steal(P,T) :-  
    thief(P),  
    likes(P,T).
```

Stealing

Example (thief.pl)

```
thief(john).  
likes(mary, food).  
likes(mary, wine).  
likes(john, X) :-  
    likes(X, wine).  
may_steal(X, Y) :-  
    thief(X),  
    likes(X, Y).
```

Demo thief.pl.

▶ `?- may_steal(john, X).`