

Every Polynomial Ideal is Finitely Generated

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Scientific Goals and Methods

$$\left(1 - t\left(\frac{1}{x} + \frac{1}{y} + xy\right)\right) f(t, x, y) = 1 - \frac{1}{y}t f(t, x, 0)$$

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$$\implies f(t, x, y) = \frac{2x^2yt - x + t + \sqrt{(x-t)^2 - 4t^2x^3}}{2x^2yt\left(1 - t\left(\frac{1}{x} + \frac{1}{y} + xy\right)\right)}$$

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Kernel method \implies

$$f(t, x, y) = \frac{2x^2yt - x + t + \sqrt{(x-t)^2 - 4t^2x^3}}{2x^2yt\left(1 - t\left(\frac{1}{x} + \frac{1}{y} + xy\right)\right)}$$